



equilibrium θ_0
 SH motion ω .

at θ_0 , Forces balance

$$N = mg \cos \theta_0$$

$$\mu N = mg \sin \theta_0$$

$$\mu = mg \tan \theta_0 \rightarrow \tan \theta_0 = \frac{\mu}{mg} \quad \text{determines } N \text{ too.}$$

~~$$N_z = mg \cos(\theta + \theta_0)$$~~

~~$\frac{\mu N_z}{N}$~~ at $\theta \neq \theta_0$, $\theta > \theta_0$ wlog,

negative

$$\mu N - mg \sin \theta = \vec{F} = m r \ddot{\theta}$$

$$mg (\sin \theta_0 - \sin \theta) = m r \ddot{\theta}$$

$$\sin(\theta_0 - \theta) \cos \theta = \frac{r \ddot{\theta}}{g}$$

~~$$\sin(\theta_0 - \theta) \cos \theta_0 = \frac{r \ddot{\theta}}{g}$$~~

~~$$\rightarrow \frac{r}{g \cos \theta_0} \ddot{\theta} + \theta = \theta_0 \cos \theta_0$$~~

$$\ddot{\theta} + \frac{g \cos \theta_0}{r} \theta = \theta_0 \cos \theta_0$$

$$\omega^2 = \frac{g \cos \theta_0}{r}$$

$$= \frac{g \mu g}{r \sqrt{(mg)^2 + \mu^2}}$$

$$\sin(\theta_0 - \theta + \theta) \cos \theta + \sin \theta_0 \cos(\theta_0 - \theta)$$

$$\sin((\theta - \theta_0) + \theta_0)$$

$$\sin \theta = \sin(\theta - \theta_0) \cos \theta_0 + \sin \theta_0 \cos(\theta - \theta_0)$$

$$\Rightarrow (\theta - \theta_0) \cos \theta_0 + \sin \theta_0$$

$$\cos((\theta - \theta_0) + \theta_0)$$

$$\cos(\theta - \theta_0) \cos \theta_0 - \sin(\theta - \theta_0) \sin \theta_0$$

$$\cos \theta_0 - (\theta - \theta_0) \sin \theta_0$$

where $\tan \theta_0 = \frac{\mu}{mg}$

